# Femoral Torsion in CT: Why We Should Add Some Trigonometry 

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Received: December 31, 2020; Accepted: J anuary 25, 2021; Published: February 01, 2021


#### Abstract

Purpose: In our department, we routinely perform Computed Tomography (CT) or Magnetic Resonance Imaging (MRI) of the lower extremity to assess femoral torsion for preoperative planning prior correcting osteotomies. It might be difficult to assess the FA, because on axial images the depicted part of the femoral neck is too short to allow correct alignment of the axis of the femoral neck. Measurements can also be performed on oblique axial images with improvement of depiction of the femoral neck but are smaller than those of measurements on axial images, due to the fact that images depend on rules of trigonometry. The aim is to provide a trigonometrical formula to calculate the value for FA, allowing precise assessment of femoral anteversion on oblique axial images similar to those on axial images.


Materials and Methods: Trigonometrical transformation is performed in three steps. Initial measurement of femoral anteversion on oblique images is transformed via a corresponding rectangular triangle from coronal images to calculated femoral anteversion on axial images.

Results: The first triangle is labelled with a1, b1, c1 for the sides and alpha1, beta1 for the angles. Second and third triangle is labelled correspondingly. Length of both cathetus a1 and b1 are calculated as follows: cathetus a1=sin alpha1*c1 and cathetus b1=cos alpha $1^{*} c 1$. Cathetus b2 is calculated as follows: $\mathrm{b} 2=\cos$ alpha2*${ }^{*} 2$. alpha3 $=\tan ^{-1}(\mathrm{a} 3 / \mathrm{b} 3)$. Initial calculation of angle alpha3=$=\tan ^{-1}$ $(a 3 / b 3)=\tan ^{-1}(a 1 / b 2)$, with $a 3=a 1=\sin$ alpha1*c1 and $b 3=b 2=c o s$ alpha2*b1*c, with $b 1=\cos$ alpha1*c1 and $b 3=\cos$ alpha2* $\cos$ alpha1* $1^{2}$. The final formula is then: alpha3 $=\tan ^{-1}\left(\left(\sin\right.\right.$ alpha1 $\left.{ }^{*} 1\right) /\left(\cos\right.$ alpha2** $\cos$ alpha1 $\left.\left.{ }^{*} 1^{2}\right)\right)=\tan ^{-1}((\sin$ alpha1/(alpha2*cos alpha1*c1))

Conclusion: In this study we can provide a formula: alpha3= $\tan ^{-1}$ ((sin alpha1/(cos alpha2*cos alpha1*c1)), which allows to calculate the femoral anteversion for true axial reconstructed images with the increased accuracy of measurements on oblique images and the ability to use the already known reference values from the literature.

Keywords: Femoral torsion; Imaging; MRI; CT

## Introduction

Abnormal torsion of the femur can lead to a disturbed gait [1,2] and early onset osteoarthritis $[3,4]$ with pain and diminished quality of life [5-7]. It can be treated surgically with osteotomies [1,4,5,8]. Computed Tomography (CT) or Magnetic Resonance Imaging (MRI) of the lower extremity is routinely performed to assess femoral torsion for preoperative planning prior correcting osteotomies [9-11]. Initially the anteversion of the Femoral Neck (FA) was assessed with radiographs by an anteroposterior view of the pelvis and a Dunn view where the Collum Diaphysis Angle (CCD) and projected femoral anteversion were measured and true FA was calculated [12,13]. Later Strecker et al. proposed the use of CT to measure Femoral Torsion (FT) [9]. In this method the FA and the rotation of the femoral condyles is measured on axial images and FT is calculated. Normal values could be established in a large patient group of 505 [9]. In patients with larger CCD angles it might be difficult to assess the FA, because on axial images the depicted part of the femoral neck is too short to allow
correct alignment of the axis of the femoral neck [10,14]. In studies by Tomczak et al., and Schneider et al., measurements for the femoral neck were performed on oblique axial images with improvement of depiction of the femoral, neck and measurements of FA were considered to be more accurate $[10,14]$. But the values for FA were smaller than those of the classic measurement introduced by Strecker et al., $[10,14]$. This is due to the fact that images in MRI or CT are also projections and depend on rules of trigonometry, already shown by Sutter et al., who transformed measurements of femoral anteversion from oblique images to axial projections and tried to establish normal values for FA and FT on oblique axial images [15]. The hypothesis of our study is that we can provide a trigonometrical formula to calculate the value for FA, equivalent to those on axial images from measurements on oblique axial images and coronal scout images. The aim of the study is to allow precise assessment of femoral anteversion on oblique axial images without the need to establish new normal values.

## Methods and Material

Institutional Review Board approval was waived due to the technical aspects of the study. For illustrational purpose three wooden models of the proximal femur with true CCD angles of $120^{\circ}$, $130^{\circ}$ and $150^{\circ}$ were built. To simulate anteversion also three wedges were built with $10^{\circ}, 20^{\circ}$ and $30^{\circ}$ increment. All models were scanned with a CT scanner (Siemens Healthineers). Each data set consists of scout images and reconstructed images in true axial orientation and oblique images aligned to the CCD angle of each model.

To illustrate the path of trigonometrical transformation of the anteversion of the femoral neck on oblique images to anteversion on true axial images is divided into three steps. Angles are measured between the axis of the femoral neck through the center of the femoral head and a horizontal. The first triangle (Figure 1) is defined by the projected increment of axis of the femoral neck, and the length of the femoral neck on oblique images. The measurement of length of the femoral neck is performed similar to the measurement of Strecker et al., from the center of the femoral neck along the axis of the femoral neck to the line connecting the anterior and posterior outline of the lesser trochanter [9]. The second triangle (Figure 2) is defined by the measurement of the projected CCD angle on true coronal scout images and calculated values for the other two angles and sides of the triangle. The third triangle (Figure 3) represents the triangle on true axial images defined by the projected increment of the femoral neck, the projected length of the femoral neck and the height of the center of the femoral head, and is calculated of values from the first and second triangle. The connection of these three triangles is demonstrated (Figure 4)

## Results

With the CT data sets, the influence of rotation on the projected CCD angle is shown. For the model with a true CCD angle of $120^{\circ}$ the projected CCD angle can range from $120^{\circ}$ to $180^{\circ}$ in different views from perpendicular to parallel to the femoral neck. In the model with a true CCD angle of $150^{\circ}$ the projected angle can range from $150^{\circ}$ to $180^{\circ}$ (Figure 5). The influence of the orientation of reconstructed planes on the measured increment/anteversion of the femoral neck is demonstrated in (Figure 6). It is lower on oblique images than on true axial images. The transformation of values from oblique axial images to those of true axial images by using trigonometry in right-angled triangles can be divided into three steps.
A) The sides of the first triangle are labeled with al and b1 for the cathetus und cl for the hypotenuse. The corresponding angles are alphal and betal (Figure 1). The femoral neck axis is equal to hypotenuse cl and increment is angle alpha1. Length of both cathetus al and b1 are calculated as follows: cathetus al=sin alpha1 ${ }^{*} \mathrm{c} 1$ and cathetus $\mathrm{b} 1=\cos$ alpha $1^{*} \mathrm{c} 1$
B) The sides of the second triangle are labeled with a2 and b2 for the cathetus and c2 for the hypotenuse. The corresponding angles are alpha2 and beta2 (Figure 2). The cathetus b1 of the first triangle is equal to the hypotenuse c 2 of the second triangle (Figure 2). The projected CCD angle is measured on the scout image. This angle minus $90^{\circ}$ is alpha2 in the second triangle (Figure 2). Cathetus b2 is calculated as follows: $\mathrm{b} 2=\cos$ alpha2 $2^{*} \mathrm{c} 2$.


Figure 1: The first triangle is aligned along the axis of the femoral neck. The sides of the first triangle are labeled with a 1 and b 1 for the cathetus und c 1 for the hypotenuse. The corresponding angles are alpha1 and beta1. The femoral neck axis and length is equal to hypotenuse c1 and increment is angle alpha1.


Figure 2: The second triangle is orientated similar to an anteroposterior view on x-ray. The sides of the second triangle are labeled with a2 and b2 for the cathetus and c2 for the hypotenuse. The corresponding angles are alpha2 and beta2. The projected CCD angle is measured on the scout image. This angle minus $90^{\circ}$ is alpha2 in the second triangle.


Figure 3: The third triangle is aligned along the true axial orientation. The sides of the triangle are labeled with a3 and b3 for the cathetus and c3 for the hypotenuse. The corresponding angles are alpha3 and beta3. Femora anteversion similar to true axial images is represented by alpha3.

The hypotenuse c 2 of the second triangle is equal to the cathetus b 1 of the first triangle: $\mathrm{c} 2=\mathrm{b} 1$. And $\mathrm{b} 1=\cos$ alpha $1^{*} \mathrm{c}$. The angle alpha2 $=$ CCD $-90^{\circ}$. We can replace c 2 and b 1 as follows: $\mathrm{b} 2=\cos$ alpha2 $2^{*} \mathrm{c} 2=\cos$ alpha2*b1 and finally b2=cos alpha $2^{*} \cos$ alpha $1^{*} \mathrm{c} 1$
C) The sides of the third triangle are labeled with a3 and b3 for the cathetus and c3 for the hypotenuse. The corresponding angles are alpha3 and beta3 (Figure 3). Cathetus a3 is equal to a1 and cathetus b 3 is equal to b 2 . Femoral anteversion similar to true axial images is represented by alpha3 (Figure 3). The tan alpha3=a3/b3. The angle alpha3 is then calculated as follows:

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alpha3=}=\mp@subsup{\operatorname{tan}}{}{-1}(\textrm{a}3/\textrm{b}3
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The cathetus a3 is equal to al and cathetus b3 is equal to b2. We can replace a 3 and b 3 as follows: alpha3 $=\tan ^{-1}$ (a1/b2)


Figure 4: Combination of all 3 triangles: The triangle on top is the first triangle. In the middle is triangle 2 and at the bottom is triangle 3. The cathetus b 1 of the first triangle is equal to the hypotenuse c 2 of the second triangle. Cathetus a3 is equal to a 1 and cathetus b 2 is equal to cathetus b 3 . This figure also shows that the femoral length c1 measured on oblique axial images is different to the femoral length c 3 measured on true axial images.


Figure 5: Dependence of CCD angle due to rotation: Three-dimensional volume rendering of wooden models show dependence of projected Collum Diaphysis Angle (CCD) to viewing angle.
A: Wooden model with $120^{\circ}$ CCD. The viewing angle is perpendicular to the surface of the femoral neck. Thus the projected CCD is equal to the true CCD of $120^{\circ}$.
B: In the same model, the viewing angle is now along the femoral neck and the projected CCD is $180^{\circ}$.
C and D: Showing the same effect for a wooden model with a CCD of $140^{\circ}$
After condensing the three steps into one formula, the femoral anteversion on axial images can be calculated from the measurement of the length of the femoral neck on oblique images, the anteversion of the femoral neck on oblique images and the projected CCD angle on scout images as shown.

Initial calculation of angle alpha3 $=\tan ^{-1}(\mathrm{a} 3 / \mathrm{b} 3)=\tan ^{-1}(\mathrm{a} 1 / \mathrm{b} 2)$
a3 $=\mathrm{a} 1=\sin$ alpha1 ${ }^{*} \mathrm{c} 1$
b3=b2=cos alpha2 ${ }^{*} \mathrm{~b} 1^{*} \mathrm{c} 1$
with $\mathrm{b} 1=\cos$ alpha1 ${ }^{*} \mathrm{cl}$
b3=cos alpha2 $2^{*} \cos$ alpha1 ${ }^{*}{ }^{*} 1^{2}$
The final formula is then:
alpha3 $=\tan ^{-1}\left(\left(\sin\right.\right.$ alpha1 $\left.1^{*} \mathrm{c} 1\right) /\left(\cos\right.$ alpha2 $2^{*} \cos$ alpha1 $\left.\left.1^{*} \mathrm{c}^{2}\right)\right)$

$$
=\tan ^{-1}\left(\left(\sin \text { alpha1 } /\left(\cos \text { alpha2 } 2^{*} \cos \text { alpha1 * } \mathrm{c} 1\right)\right)\right.
$$

In this formula, alpha1 is the measured anteversion of the femoral neck on oblique images. Alpha2 is the measured CCD angle minus $90^{\circ} . \mathrm{C} 1$ is the measured length of the femoral neck. When using this formula it is necessary to know that the value of tangens always


Figure 6: Dependence of anteversion from oblique to axial: Multiplanar reconstructions of a wooden model with known length of the femoral neck of 10 cm and a CCD of $120^{\circ}$. The model was scanned on a wedge with an anteversion of $22^{\circ}$.
A: shows the reconstructed plane in oblique orientation along the axis of the femoral neck. Length is 10 cm and similar to the true length, the projected anteversion is with $15^{\circ}$ lower than the true anteversion.
B: shows the reconstructed plane in true axial orientation of the same wooden model from the same CT scan. The projected length is with 8 cm shorter than the true length. The anteversion is $20^{\circ}$ and similar to the anteversion of the wedge.
represents 2 angles. One smaller $90^{\circ}$ and one larger $90^{\circ}$. When using a calculator or inserting the formula into a table calculating program it is necessary to define the range from $0-90^{\circ}$ to get the correct result.

## Discussion

There are numerous causes for abnormal torsion of the femur [ 16,17 ]. Abnormal torsion can lead to gait disturbances, pain and early osteoarthritis [1-7]. We routinely perform MRI or CT to assess femoral torsion. This method was introduced by Strecker et al., where the anteversion of the femoral neck and of the femoral condyles is measured, and femoral torsion can be calculated. With this method there are well established normal values allowing the diagnosis of increased or decreased femoral torsion [9]. These measurements help orthopeadic surgeons to plan correcting osteotomies [4,5,9,13,16]. Since introduction of measurements of the femoral torsion the high inter-observer variability is discussed [10,11,14,15]. This may be due to the fact, that in patients for example with coxa valga, who have large CCD angles, the depicted portion of the femoral neck is short and correct measurement of the axis is difficult to achieve. This is especially true in children and adolescent patients, since the CCD angle decreases with age from $150^{\circ}$ to $130^{\circ}[18,19]$. Tomczak et al., and Schneider et al., introduced a variation of assessing the femoral neck, by using oblique axial images of the femoral neck in MRI $[10,14]$. In these studies it was possible to depict the whole femoral neck on one image and to increase interobserver reliability of measurements of the femoral neck anteversion $[10,14]$. The authors also noticed an overall decrease of the femoral anteversion in their study population [10,14]. This was considered to be a bias of the patient group and lastly remained incompletely explained $[10,14]$. We assume that in this study the effects of trigonometry were underestimated. As we could show in our wooden models these effects cannot be neglected. Depending on the viewing angle, the visible angle can range from the true CCD angle to a maximum of $180^{\circ}$ (Figure 5). This is also true for the measurement of the anteversion of the femoral neck on oblique images and axial images on the same model with the same true anteversion (Figure 6). In our opinion, a transformation of measurements on oblique images to values on axial images would be helpful, because there are well-established reference values in large patient groups allowing comparison of measurements on
oblique images with these reference values. Thus, establishment of new references could be omitted. In a study by Sutter et al., the trigonometrical transformation of measurements of the femoral anteversion from oblique to axial images was performed [15]. Sutter et al., tried to establish normal values for measurements on oblique images. But the patient group was smaller than those in prior studies In their study, the final formula to calculate the anteversion does not contain the length of the femoral neck. This is in contrast to our results where the length is necessary to calculate the femoral anteversion on true axial images. In this study we can provide a formula: alpha3 $=\tan ^{-1}$ ((sin alpha1/(cos alpha2 ${ }^{*}$ cos alpha1 ${ }^{*}$ c1)), which allows to calculate the femoral anteversion for true axial reconstructed images with the increased accuracy of measurements on oblique images and the ability to use the already known reference values from the literature.

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